

Spring 2024

## BIOS 477/877

### *Bioinformatics and Molecular Evolution*

## Lecture 19

BIOS477/877 L19 - 1

1

## TODAY'S TOPICS

- Protein family/domain databases (InterPro, SMART, etc.)
- Distance estimation
  - Nucleotide substitutions

BIOS477/877 L19 - 2

2

InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

**[Member databases]**

**[Other information]**

Other sequence features:  Prokts  SignalP  Coils  MobiLite  TMHMM

Other category:  SignalP\_EAK  SignalP\_GRAM\_POSITIVE  SignalP\_GRAM\_NEGATIVE  Jaxfam  Funfam  PIRSF

Domains will be searched against all these databases

Transmembrane, signal peptide, coils, disordered regions will be predicted

BIOS477/877 L19 - 3

3

InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

To browse each member database (Pfam, etc.)

InterPro is the new home of Pfam. The Pfam website (pfam.xfam.org) was shut down on October 5th, but InterPro offers the same functionality and data. A legacy version of Pfam is available at <https://pfam-legacy.xfam.org/> (but will not receive any updates and will be decommissioned in Spring 2023).

Search by sequence, Search by Domain Architecture

Sequence, in FASTA format

Enter your sequence

Choose file Example protein sequence

Advanced options

Powered by InterProScan  
BIOS477/877 L19 - 4

4

InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

**[Pfam database entries]**

Accession	Name	Pfam Type	OR	INTEGRATED DATA
PF00001	7 transmembrane receptor (rhodopsin family)	family		IPR000276
PF00002	7 transmembrane receptor (Secretin family)	family		IPR000832
PF00003	7 transmembrane sweet-taste receptor of 3 GPCR	domain		IPR017978
PF00004	ATPase family associated with various cellular activities (AAA)	domain		IPR003959
PF00005	ABC transporter	domain		IPR003439

BIOS477/877 L19 - 5

5

InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

InterPro is the new home of Pfam. The Pfam website (pfam.xfam.org) was shut down on October 5th, but InterPro offers the same functionality and data. A legacy version of Pfam is available at <https://pfam-legacy.xfam.org/> (but will not receive any updates and will be decommissioned in Spring 2023).

Search by sequence, Search by text, Search by Domain Architecture

Sequence, in FASTA format

Enter your sequence

InterProScan

Choose file Example protein sequence

Advanced options

Powered by InterProScan  
BIOS477/877 L19 - 6

6

**InterPro** Classification of protein families

Protein family membership

Entry matches to this protein

Representative Domains

Family

Domain

Homologous Superfamily

Conserved Site

Unintegrated

Other Features

**InterPro integrates many domain and other protein functional information:**

IPR: InterPro  
PF: Pfam  
SSF: SUPERFAMILY  
PTHR: PANTHER  
SM: SMART  
PS: PROSITE

<https://www.ebi.ac.uk/interpro/> BIOS477/877 L19 - 7

7

**InterPro** Classification of protein families

Protein family membership

Entry matches to this protein

Representative Domains

Family

Domain

Homologous Superfamily

Conserved Site

Unintegrated

Other Features

**Transmembrane region predictions**

<https://www.ebi.ac.uk/interpro/> BIOS477/877 L19 - 8

8

**InterPro/Pfam family/domain information**

InterPro Classification of protein families

Home Search Browse Results Release notes Download Help About

/ Browse / By Entry / Pfam / PF12704 / Overview

**Pfam** MacB-like periplasmic core domain PF12704

Member database Pfam

Overview

Proteins 202k

Domain Architectures 214

Taxonomy 37k

Protomes 8k

Structures 27

Signature

AlphaFold 170k

Alignment

Curation

Description

This family represents the periplasmic core domain found in a variety of ABC transporters. The structure of this family has been solved for the MacB protein [PMID:19432486]. Some structural similarity was found to the periplasmic domain of the AcrB multidrug efflux transporter.

<https://www.ebi.ac.uk/interpro/> BIOS477/877 L19 - 9

9

**InterPro/Pfam family/domain information**

InterPro Classification of protein families

Home Search Browse Results Release notes Download Help About

/ Browse / By Entry / Pfam / PF12704 / Domain Architecture

**Pfam** MacB-like periplasmic core domain PF12704

214 domain architectures found.

Overview

Proteins 393k

Domain Architectures 214

Taxonomy 37k

Protomes 8k

Structures 27

Signature

AlphaFold 370k

Alignment

Curation

There are 328713 proteins with this architecture (represented by P44250): PF12704 - PF02687 - MacB\_PCD

There are 26264 proteins with this architecture (represented by Q9K3M9): PF12704 - PF02687 - PF12704 - PF02687 - F1xK

There are 20416 proteins with this architecture (represented by Q9WZ05): PF12704 - PF02687 - PF02687 - MacB\_PCD - F1xK

There are 9294 proteins with this architecture (represented by P94999): PF12704 - MacB\_PCD

There are 8756 proteins with this architecture (represented by P75833): PF00005 - PF12704 - PF02687 - ABC\_tran - MacB\_PCD - F1xK

There are 6784 proteins with this architecture (represented by Q9L0K3): PF02687 - PF12704 - PF02687 - F1xK - MacB\_PCD

**These are the proteins that have a given domain (PF12704) as well as other domains**

<https://www.ebi.ac.uk/interpro/> BIOS477/877 L19 - 10

10

**InterPro/Pfam family/domain information**

InterPro Classification of protein families

Home Search Browse Results Release notes Download Help About

/ Browse / By Entry / Pfam / PF12704 / Curation

**Pfam** MacB-like periplasmic core domain PF12704

Overview

Proteins 202k

Domain Architectures 214

Taxonomy 37k

Protomes 8k

Structures 27

Signature

AlphaFold 170k

Alignment

Curation

**Profile HMM logo (signature)**

Letter height  $\propto$  letter frequency

Stack height:  $\sum_{i=1}^{20} p_i \log_2(P_i/q_i)$

For each column,  $p_i$ : Probability of AA,  $q_i$ : Background distribution of AA

Information Content (bits)

Occupancy

Insert Probability

Expected Insert length

Orange  $\rightarrow$  more insertions

Blue  $\rightarrow$  more deletions

<https://www.ebi.ac.uk/interpro/> BIOS477/877 L19 - 11

11

**InterPro/Pfam family/domain information**

InterPro Classification of protein families

Home Search Browse Results Release notes Download Help About

/ Browse / By Entry / Pfam / PF12704 / Curation

**Pfam** MacB-like periplasmic core domain PF12704

Overview

Proteins 202k

Domain Architectures 214

Taxonomy 37k

Protomes 8k

Structures 27

Signature

AlphaFold 170k

Alignment

Curation

Author Bateman

Sequence Ontology SO:0100021

HMM Information

HMM build commands Build method: hmmbuild -o /dev/null HMM SEED Search method: hmmscan -Z 61295632 -E 1000 -cpu 4 HMM pfamseq

Gathering threshold Sequence: 27 Domain: 27

Download

Download the raw HMM for this family

<https://www.ebi.ac.uk/interpro/> BIOS477/877 L19 - 12

12

## Profile HMM entry

HMMSER# [3,1b2] | February 2015  
 NAME: Mac2\_P20  
 ACC: PF12704.10  
 DESC: Mac2-like peripla  
 LENG: 196  
 ALPH: amino  
 BE: no  
 RM: no  
 COMS: yes  
 CS: no  
 MAP: yes  
 DATE: Tue Oct 12 12:48:  
 NSEQ: 503  
 EFIN: 10.979383  
 CKSUM: 1075013902  
 GA: 27 27:  
 TC: 27 27:  
 NC: 21 0 26 0  
 NI: nonebuild HM.ann SEED.ann  
 SR: hmmsrch2-2 61295633 -E 3000 -cdu 4 HMH prmsseq  
 STATS LOCAL MSV -19.1794 0.78560  
 STATS LOCAL VITERBI -12.0228 0.78560  
 STATS LOCAL FORWARD -4.2228 0.78560  
 HMM:

**For each site:**  
 1st line → Emission probabilities (20 aa) for match state  
 2nd line → Emission probabilities (20 aa) for insertion state  
 3rd line → Transition probabilities  
 \*Probability in -log(Prob): if Prob = 1 (fully conserved), -log(1) = 0 (smaller for more conserved)

**Transition probability legend**  
 (m: match, i: insertion, d: deletion)

	a	c	d	e	f	g	h	i	k	l
COMP0	2.43923	5.00205	2.94999	2.49335	3.29432	2.55744	4.13874	2.74608	2.95946	2.47214
2.68618	4.42225	2.77519	2.73123	3.46354	2.48513	3.72494	3.29354	2.67741	2.69355	
0.98199	6.61837	7.34872	6.61958	6.77255	6.88880					
2.56721	3.18157	5.78148	3.14804	3.23165	4.24888	0.46769	3.85447	4.72164	2.33118	
2.68618	4.42225	2.77519	2.73123	3.46354	2.48513	3.72494	3.29354	2.67741	2.69355	
0.98199	6.61837	7.34872	6.61958	6.77255	6.88880					
2.16548	4.39125	5.99017	3.37973	1.76631	3.16952	5.51657	2.38546	5.15514	1.57311	
2.68618	4.42225	2.77519	2.73123	3.46354	2.48513	3.72494	3.29354	2.67741	2.69355	
0.98199	6.61837	7.34872	6.61958	6.77255	6.88880					
3.14358	4.92185	5.99355	3.37741	1.36974	3.02115	5.55800	2.84681	5.15984	8.72146	
2.68622	4.42229	2.77523	2.73127	3.46358	2.48516	3.72498	3.29358	2.67744	2.69359	
0.98208	6.61892	7.34877	6.62038	6.77257	6.88976					
4.166579	5.23984	5.73735	5.13656	4.12181	4.86484	5.12921	3.39641	4.96922	3.11169	
4.68618	4.42225	2.77519	2.73123	3.46354	2.48513	3.72494	3.29354	2.67741	2.69355	
0.98199	6.61837	7.34872	6.61958	6.77255	6.88878					
5.249746	6.91784	6.83923	6.82508	6.21021	5.29568	5.57689	1.54711	5.28979	1.96913	
2.68618	4.42225	2.77519	2.73123	3.46354	2.48513	3.72494	3.29354	2.67741	2.69355	
0.98199	6.61837	7.34872	6.61958	6.77255	6.88876					
2.51298	5.81337	5.99125	3.37513	1.56741	3.25466	5.51687	3.17693	5.15712	8.66616	
2.68618	4.42225	2.77519	2.73123	3.46354	2.48513	3.72494	3.29354	2.67741	2.69355	
0.98199	6.61837	7.34872	6.61958	6.77255	6.88880					

BIOS477/877 L19 - 13

13

## InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

InterPro is the new home of Pfam  
 The Pfam website (www.pfam.org) was shut down on October 5th, but InterPro offers the same functionality and data. A legacy version of Pfam is available at <https://pfam-legacy.xfam.org/> (but will not receive any updates and will be decommissioned in Spring 2023).

Search by sequence | Search by text | **Search by domain architecture**

Sequence, in FASTA format

Enter your sequence

# InterProScan

Choose file | Example protein sequence

Advanced options

Powered by InterProScan

BIOS477/877 L19 - 14

14

## InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

Search InterPro

Search for proteins with a specific domain architecture

Domain architectures are derived from matches to Pfam models. You can select domains to either be included or excluded from your search results. The results will include all proteins which match the domain architecture selected below. Domains can be selected using either a Pfam accession, or an InterPro accession, where that InterPro entry includes a Pfam model.

**Architectures must include**

**Architectures must not include**

Add Domain to include | Add Domain to exclude

Order of domain matters: Yes | No  
 Exact match: Yes | No

BIOS477/877 L19 - 15

15

## InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

Search InterPro

Search for proteins with a specific domain architecture

Domain architectures are derived from matches to Pfam models. You can select domains to either be included or excluded from your search results. The results will include all proteins which match the domain architecture selected below. Domains can be selected using either a Pfam accession, or an InterPro accession, where that InterPro entry includes a Pfam model.

**Architectures must include**

**Architectures must not include**

Add Domain to include | Add Domain to exclude

Order of domain matters: Yes | No  
 Exact match: Yes | No

**4 domain architectures found.**

There are 4 proteins with this architecture represented by UniProt

There are 4 proteins with this architecture represented by UniProt

BIOS477/877 L19 - 16

16

## InterPro Classification of protein families

<https://www.ebi.ac.uk/interpro/>

Search InterPro

Search for proteins with a specific domain architecture

Domain architectures are derived from matches to Pfam models. You can select domains to either be included or excluded from your search results. The results will include all proteins which match the domain architecture selected below. Domains can be selected using either a Pfam accession, or an InterPro accession, where that InterPro entry includes a Pfam model.

**Architectures must include**

**Architectures must not include**

Add Domain to include | Add Domain to exclude

Order of domain matters: Yes | No  
 Exact match: Yes | No

**1 domain architectures found.**

There is 1 protein with this architecture represented by UniProt

BIOS477/877 L19 - 17

17

## Profile HMM search by HMMER

<https://www.ebi.ac.uk/Tools/hmmer/>

HMMER  
 Biosequence analysis using profile hidden Markov Models

Quick search = **phmmer**

Paste in your sequence or use the example

Enter your sequence

Reference Proteomes | UniProtKB | SwissProt | Pfam

Download HMMER v3.3.2

News | February 2022 | Download HMMER v3.3.2

Papers

HMMER web server: 2018 updated

BIOS477/877 L19 - 18

18

## Profile HMM search by HMMER

<https://www.ebi.ac.uk/Tools/hmmer/>

Like blastp → hmmer  
Like PSI-blast → jackhammer

query: protein sequence(s)  
database: proteins profile HMMs proteins

BIOS477/877 L19 - 19

19

## HMMER hmmscan result

Disorder, coiled-coil, transmembrane regions, and signal peptide predictions are also done

Active site

Sequence Matches and Features

Available cross-references at the EBI (powered by EBI Search):

BIOS477/877 L19 - 19

20

## HMMER hmmscan result

Advanced view

$\log_2 \frac{P(seq|HMM)}{P(seq|null)}$

Domain family | Clan: a collection of families

BIOS477/877 L19 - 21

21

## NCBI Conserved Domains

<https://www.ncbi.nlm.nih.gov/Structure/cdd/wrpsb.cgi>

Search for Conserved Domains within a protein or coding nucleotide sequence

Enter protein or nucleotide query as accession, gi, or sequence in FASTA format. For multiple protein queries, use Batch.

Options: Search against database: CDD v3.20 - 59933 PSSMs, Expect Value threshold: 0.00001, Apply low-complexity filter, Composition based statistics adjustment, Force the search, Rescue borderline hits, Suppress weak overlapping hits, Maximum number of hits: 600, Result mode: QConcise, Standard, Full.

Retrieve previous CD-search result

BIOS477/877 L19 - 22

22

## NCBI Conserved Domains

<https://www.ncbi.nlm.nih.gov/Structure/cdd/wrpsb.cgi>

Conserved domains on [dcl:seqip\_MACFS\_dcl2256969/801396b1888ea075c0de]

Graphical summary

Specific hits

List of domain hits

References:

https://www.ncbi.nlm.nih.gov/Structure/cdd/wrpsb.cgi

BIOS477/877 L19 - 23

23

## NCBI CONSERVED Domain Architecture Retrieval Tool

Enter your results:

List of domain architectures

BIOS477/877 L19 - 24

24



### HHblits: lightning-fast iterative protein sequence searching by HMM-HMM alignment

Michael Remmert, Andreas Biegert, Andreas Hauser & Johannes Söding

*Nature Methods* 9, 173–175 (2012) | [Cite this article](#)

<https://toolkit.tuebingen.mpg.de/hhblits>

- Convert the query sequence to a profile HMM by adding context-specific pseudocounts
- HMM-HMM search against an HMM database (e.g., generated from clustered UniProt at 20% similarity; UniProt20)
- Sequences from the accepted HMMs are iteratively added to the query sequences

BIOS477/877 L19 - 31

31

### HHblits: lightning-fast iterative protein sequence searching by HMM-HMM alignment

Michael Remmert, Andreas Biegert, Andreas Hauser & Johannes Söding

*Nature Methods* 9, 173–175 (2012) | [Cite this article](#)

<https://toolkit.tuebingen.mpg.de/hhblits>

Fast search comparing sequences coded into 219 letters

219-letter profile

219 profile codes

Each position of MSA is coded into single letter

MSA + pseudocounts

Query/DB MSA

BIOS477/877 L19 - 32

32

BMC Bioinformatics

SOFTWARE Open Access

### HH-suite3 for fast remote homology detection and deep protein annotation

Martin Steinegger<sup>1,2</sup>, Markus Meier<sup>1</sup>, Milot Mirdita<sup>1</sup>, Harald Vöhringer<sup>1,3</sup>, Stephan J. Haubertberger<sup>4</sup> and Johannes Söding<sup>1\*</sup>

Time (sec)

Number of iterations

Fraction of queries

AUC up to the first false positive

More accurate

<https://toolkit.tuebingen.mpg.de/hhblits>

BIOS477/877 L19 - 33

33

### Distance estimation

Ancestral sequence ?

ACTGTAGGAATCGC AATGAAAGAATCGC

S1 ← Amount of evolution → S2

Distance

S1 ACTGTAGGAATCGC  
:X::X:X::: (No. of differences = 3)

S2 AATGAAAGAATCGC

BIOS477/877 L19 - 34

34

### Distance estimation

➤ The simplest method (*p*-distance)

→ Number of substitutions per site (*p*) or degree of divergence

$$p = \frac{n_d}{L} \quad V(p) = \frac{p(1-p)}{L} \quad \text{or} \quad \sigma(p) = \sqrt{\frac{p(1-p)}{L}}$$

*n<sub>d</sub>*: Number of differences between the two sequences  
*L*: Number of nucleotides (or amino acids) compared  
*V*(*p*), *σ*(*p*): Variance or standard error of the mean (*p*) for binomial distribution

→ Can be used for both nucleotide and amino acid substitutions

ACTGTAGGAATCGC     *n<sub>d</sub>* = 3, *L* = 14  
 :X::X:X:::     *p* = 3/14 = 0.214  
 AATGAAAGAATCGC     *σ<sub>p</sub>* = √{(0.214x(1-0.214)/14)} = 0.110  
    *p* = 0.214 ± 0.110

BIOS477/877 L19 - 35

35

### Distance estimation

Ancestral sequence ?

ACTGTAGGAATCGC AATGAAAGAATCGC

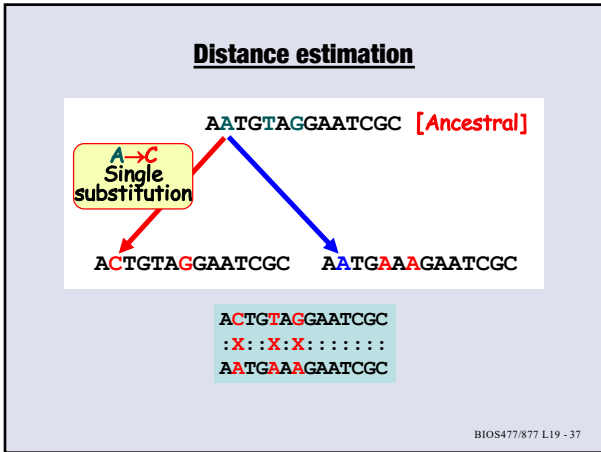
S1 ACTGTAGGAATCGC  
:X::X:X::: (No. of differences = 3)

S2 AATGAAAGAATCGC

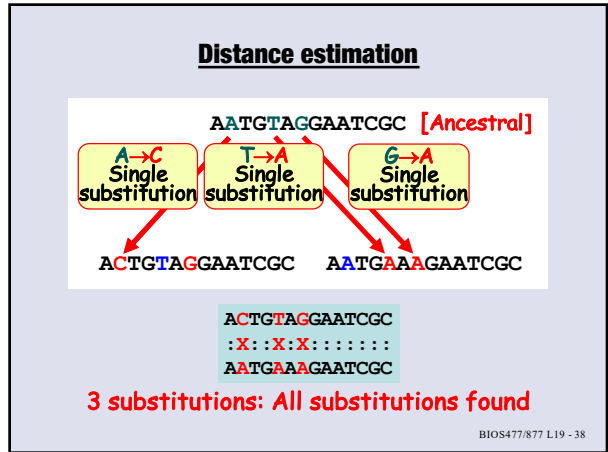
Were there only three changes during the evolution?

BIOS477/877 L19 - 36

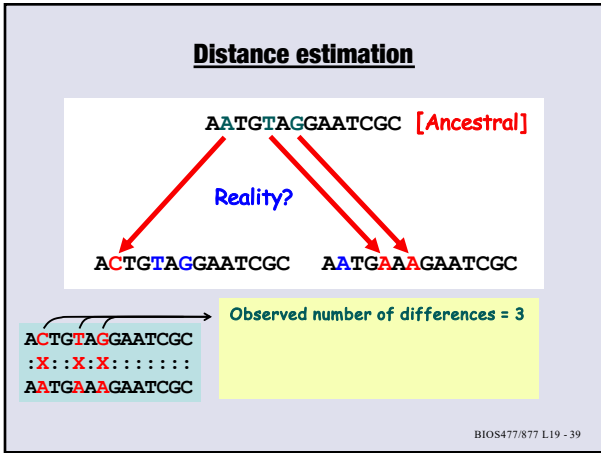
36



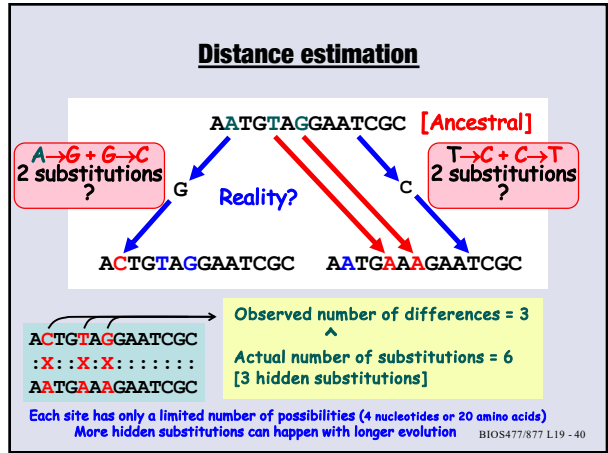
37



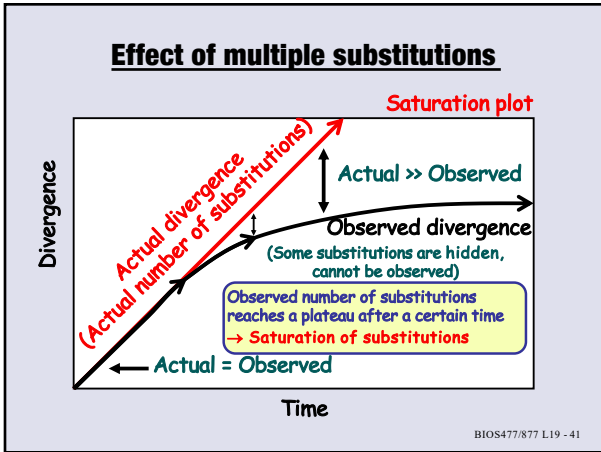
38



39



40



41

- ### Effect of multiple substitutions
- When the degree of divergence between two sequences is small,
    - the chance of having more than one substitution at any site is negligible
    - Observed divergence ≈ actual divergence
  - When the degree of divergence becomes larger,
    - more than one substitution could happen at any site
    - [multiple substitutions or multiple hits]
    - Observed divergence << actual divergence [Saturation effect]
  - Effect of multiple hits is larger for nucleotide substitutions
  - Methods to uncover the number of hidden substitutions need to be used [Multiple hit correction]
    - Actual divergence level is estimated based on the observed degree of divergence
- BIOS477/877 L19 - 42

42

### Distance estimation for nucleotide substitutions

➤ **Jukes-Cantor (one-parameter) method** Jukes and Cantor (1969)

	A	C	G	T
A	-	$\alpha$	$\alpha$	$\alpha$
C	$\alpha$	-	$\alpha$	$\alpha$
G	$\alpha$	$\alpha$	-	$\alpha$
T	$\alpha$	$\alpha$	$\alpha$	-

All substitutions occur with equal probability  
[Jukes-Cantor model of nucleotide substitutions]

(Derivation of the JC equation: a note on Canvas) BIOS477/877 L19 - 43

$$k = -\frac{3}{4} \ln\left(1 - \frac{4}{3}p\right)$$

$k$ : Expected number of nucleotide substitutions per site or **Distance**  
 $p$ : Proportion of nucleotide differences (observed)

$V(k) = \frac{9p(1-p)}{(3-4p)^2L}$   $L$ : number of nucleotide positions compared

$\sigma(k) = \frac{3}{(3-4p)} \sqrt{\frac{p(1-p)}{L}}$

43

### Distance estimation for nucleotide substitutions

`ACTGTACGAATCGC`  
`:X::X:X:::.....`  
`AATGCAGAATCGC`

Number of differences = 3  
Sequence length = 14

- Without multiple-hit correction ( $p$ -distance):  
 $p = \frac{n_d}{L}$   
 $n_d$ : number of differences,  $L$ : number of nucleotides compared  
 $p = 3/14 = 0.214$
- With multiple-hit correction by Jukes-Cantor method:  
 $k = -\frac{3}{4} \ln\left(1 - \frac{4}{3}p\right)$   
 $p$ : (Observed) proportion of nucleotide differences = 0.214  
 $k = -3/4 \ln(1 - 4 \times 0.214/3) = 0.252$

BIOS477/877 L19 - 44

44

### Distance estimation for nucleotide substitutions

BIOS477/877 L19 - 45

45

### Distance estimation for nucleotide substitutions

➤ **Kimura two-parameter method** Kimura (1980)

	A	C	G	T
A	-	$\beta$	$\alpha$	$\beta$
C	$\beta$	-	$\beta$	$\alpha$
G	$\alpha$	$\beta$	-	$\beta$
T	$\beta$	$\alpha$	$\beta$	-

$P$ : Proportion of **transitional (Ts)** differences  
 $Q$ : Proportion of **transversional (Tv)** differences

$$k = \frac{1}{2} \ln \left[ \frac{1}{(1-2P-Q)} \right] + \frac{1}{4} \ln \left[ \frac{1}{(1-2Q)} \right]$$

Difference in Ts and Tv substitutions (usually Ts > Tv) can be considered

$$V(k) = \frac{1}{L} \left[ P \left\{ \frac{1}{(1-2P-Q)} \right\}^2 + Q \left\{ \frac{1}{(2-4P-2Q)} + \frac{1}{(2-4Q)} \right\}^2 - \left[ \frac{P}{(1-2P-Q)} + \frac{Q}{(2-4P-2Q)} + \frac{Q}{(2-4Q)} \right]^2 \right]$$

$L$ : number of nucleotide positions compared BIOS477/877 L19 - 46

46

### Distance estimation for nucleotide substitutions

`ACTGTACGAATCGC`  
`:X::X:X:::.....`  
`AATGCAGAATCGC`

Number of differences = 3  
Ts = 2, Tv = 1  
Alignment length = 14

- Without multiple-hit correction ( $p$ -distance):  
 $p = \frac{n_d}{L}$   $V(p) = \frac{p(1-p)}{L}$   $p = 0.214 \pm 0.110$
- Jukes-Cantor distance:  
 $k = -\frac{3}{4} \ln\left(1 - \frac{4}{3}p\right)$   $V(k) = \frac{9p(1-p)}{(3-4p)^2L}$   $k = -3/4 \ln(1 - 4 \times 0.214/3) = 0.252 \pm 0.154$
- Kimura 2-parameter distance:  
 $k = \frac{1}{2} \ln \left[ \frac{1}{(1-2P-Q)} \right] + \frac{1}{4} \ln \left[ \frac{1}{(1-2Q)} \right]$   $P = 2/14, Q = 1/14$   
 $k = 1/2 \ln[1/(1-4/14-1/14)] + 1/4 \ln[1/(1-2/14)]$   
 $= 0.259 \pm 0.143$

$$V(k) = \frac{1}{L} \left[ P \left\{ \frac{1}{(1-2P-Q)} \right\}^2 + Q \left\{ \frac{1}{(2-4P-2Q)} + \frac{1}{(2-4Q)} \right\}^2 - \left[ \frac{P}{(1-2P-Q)} + \frac{Q}{(2-4P-2Q)} + \frac{Q}{(2-4Q)} \right]^2 \right]$$

BIOS477/877 L19 - 47

47

### Sequence evolution as Markov process

Transition probability

[Time] T1      T2      T3      T4

**Markov Chain:** a discrete-time stochastic process  
 In more general continuous-time scale,  
 → **Markov Process**

BIOS477/877 L19 - 48

48



### Sequence evolution as Markov process

Transition probability

A →<sup>P<sub>1</sub></sup> G →<sup>P<sub>2</sub></sup> G →<sup>P<sub>3</sub></sup> A

[Time] T1 T2 T3 T4

	A	C	G	T
A	-	α	α	α
C	α	-	α	α
G	α	α	-	α
T	α	α	α	-

Jukes-Cantor model (α: substitution rate)

Transition probability matrix

$$P(t) = \begin{bmatrix} r_t & s_t & s_t & s_t \\ s_t & r_t & s_t & s_t \\ s_t & s_t & r_t & s_t \\ s_t & s_t & s_t & r_t \end{bmatrix}$$

r: Prob. of no change  
s: Prob. of changes

where  $r_t + 3s_t = 1$  (row sum)  
thus  $r_t = 1 - 3s_t$

BIOS477/877 L19 - 49

49

### Jukes-Cantor model of sequence evolution

	A	C	G	T
A	-	α	α	α
C	α	-	α	α
G	α	α	-	α
T	α	α	α	-

(e.g., α = 5x10<sup>-9</sup> substitutions/site/year)

r: Prob. of no change  
s: Prob. of changes

Probability

Time (million years)

Transition probability matrix

$$P(t) = \begin{bmatrix} r_t & s_t & s_t & s_t \\ s_t & r_t & s_t & s_t \\ s_t & s_t & r_t & s_t \\ s_t & s_t & s_t & r_t \end{bmatrix}$$

where  $r_t = \frac{1}{4} + \frac{3}{4}e^{-4\alpha t}$   
 $s_t = \frac{1}{4} - \frac{1}{4}e^{-4\alpha t}$

t=0: r<sub>0</sub>=1 & s<sub>0</sub>=0  
t→∞: r<sub>∞</sub>=0.25 & s<sub>∞</sub>=0.25

(Derivation of r, s, and J-C distance equations, read "Derivation of the JC equation" on Canvas.)

$k = -\frac{3}{4} \ln(1 - \frac{4}{3}p)$

BIOS477/877 L19 - 50

50

### Nucleotide substitution models

Jukes-Cantor (JC)  
Equal base frequency (f<sub>A</sub>=f<sub>T</sub>=f<sub>C</sub>=f<sub>G</sub>=0.25)

	A	C	G	T
A	-	α	α	α
C	α	-	α	α
G	α	α	-	α
T	α	α	α	-

Kimura 2-parameter (K2P)  
Equal base frequency (f<sub>A</sub>=f<sub>T</sub>=f<sub>C</sub>=f<sub>G</sub>=0.25)

	A	C	G	T
A	-	β	α	β
C	β	-	β	α
G	α	β	-	β
T	β	α	β	-

3-parameter model:  
Ts(A↔G), Ts(T↔C), and Tv

General reversible (REV)  
Unequal base frequency

	A	C	G	T
A	-	π <sub>CA</sub>	π <sub>GA</sub>	π <sub>TA</sub>
C	π <sub>AC</sub>	-	π <sub>GC</sub>	π <sub>TC</sub>
G	π <sub>AG</sub>	π <sub>CG</sub>	-	π <sub>TG</sub>
T	π <sub>AT</sub>	π <sub>CT</sub>	π <sub>GT</sub>	-

Felsenstein (F81)  
Unequal base frequency

	A	C	G	T
A	-	π <sub>CA}</sub>	π <sub>GA}</sub>	π <sub>TA</sub>
C	π <sub>AC}</sub>	-	π <sub>GC}</sub>	π <sub>TC</sub>
G	π <sub>AG}</sub>	π <sub>CG</sub>	-	π <sub>TG</sub>
T	π <sub>AT}</sub>	π <sub>CT</sub>	π <sub>GT</sub>	-

Hasegawa *et al.* (HKY85)  
Unequal base frequency

There are many more!

BIOS477/877 L19 - 51

51