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## Pairwise alignment summary

- Alignment score depends on:
$\rightarrow$ Scoring matrix (match, mismatch, Ts/Tv, BLOSUM, PAM, etc.) $\rightarrow$ Gap penalty
$\rightarrow$ Alignment method (e.g., global or local)
- Alignment scores cannot be compared directly $\rightarrow$ if the scoring systems used are different
$\rightarrow$ if sequences compared are different
(e.g., longer alignments tend to have higher scores)
- Alignment scores are used: for searching optimal alignments from the alignment matrix for a given pair of sequences based on a given scoring system


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## Pairwise alignment summary (continued)

- Optimal alignments and biologically meaningful alignments may not be the same
- Depending on the scoring system, unreasonable alignments can become optimal
$\rightarrow$ We need to choose a better (biologically reasonable) scoring system: level of divergence (scoring matrices), gap penalty (affine, etc.), algorithm (local, global, or semi-global)
$\rightarrow$ Manual adjustment may be necessary
$\rightarrow$ Test statistical significance of the alignment (is the alignment possible just by chance?)


## TODAY'S TOPICS

## Statistical Significance of Alignment Scores

Similarity Search

- FASTA and BLAST

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## Significance of Alignment Scores

$>$ Hypothesis testing (General)
$\rightarrow$ Two hypotheses

- Null-hypothesis
$\mathrm{H}_{0}$ : The previous (original) belief is true
- Alternative hypothesis
$\mathbf{H}_{1}$ : The previous (original) belief is false; the new theory is true
$\rightarrow S$ : Test statistic
$\rightarrow$ Significance level is chosen a priori (e.g., 0.05)
$\rightarrow P$-value: $P\left(S \mid \mathrm{H}_{0}\right.$ is true) Probability of getting $S$ if $\mathrm{H}_{0}$ is true
$\rightarrow$ If $P$ < Significance level, reject $\mathbf{H}_{\mathbf{0}}$


## Significance of Alignment Scores

$P$-value: $P\left(S \mid \mathrm{H}_{0}\right.$ is true)
$\rightarrow$ Need to be calculated from the test statistic $S$
$\rightarrow$ Need to know the probability distribution of the test statistic $S$ under $\mathrm{H}_{0}$
Central Limit Theorem:

If the sample size is large enough
the sampling distribution of
the mean of any independent,
random variables will be normal or
nearly normal.

## (Example)

Experiment: 1000 coin tossing

- Count the number of heads
- Repeat 1000 experiments
(Expect to see 500 heads/experiment)


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## Significance of Alignment Scores

$>$ Hypothesis testing for sequence alignment
$\rightarrow$ Two hypotheses

- Null-hypothesis
$\mathrm{H}_{0}$ : Two sequences are not related (random)
- Alternative hypothesis
$H_{1}$ : Two sequences are related
$\rightarrow$ Test statistic: alignment score ( $S$ )
$\rightarrow$ Significance level is chosen a priori (e.g., 0.05)
$\rightarrow P$-value: $\boldsymbol{P}\left(S \mid \mathbf{H}_{0}\right.$ is true)
Probability of getting the alignment score $S$, even if the two
sequences are not related but randomly matched
$\rightarrow$ If $P$ < Significance level, reject $\mathbf{H}_{0}$
(The score should not be obtained just by aligning unrelated sequences)

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## Significance of Alignment Scores

$>P$-value: $P\left(S \mid \mathrm{H}_{0}\right.$ is true)
$\rightarrow$ Need to be calculated from the test statistic $S$
$\rightarrow$ Need to know the probability distribution of the test statistic $S$ under $\mathbf{H}_{\mathbf{0}}$


Distribution of alignment scores follow
Extreme Value Distribution (Gumbel distribution)

The probability distribution of highest values in an experiment (e.g., optimal alignment scores)

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## Significance of Alignment Scores

$>P\left(S \geq x \mid \mathbf{H}_{0}\right)$ : Probability of getting the alignment score $S \geq x$
Karlin-Altschul equation (Karlin and Altschul 1990) $P(S \geq x)=1-\exp \left[-K m n e^{-\lambda x}\right] \approx K m n e^{-\lambda x}$
$\underset{P(S D}{ }{ }_{\text {(Gumbel distribution) }}$ $P(S \geq x)=1-\exp \left[-e^{-(x-\mu) / \beta}\right]$ $\lambda=1 / \beta, \mu=(\ln K m n) / \lambda$
$K$ and $\lambda$ : calculated from the empirical distribution of $S$ based on a given scoring matrix and amino acid composition $m$ and $n$ : lengths of sequences aligned
$\rightarrow$ Solved for ungapped local alignments $\rightarrow$ Can be applied for gapped local alignments


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>\mathrm{E} \text {-value }=P\left(S \geq x \mid \mathrm{H}_{0}\right) \times N,
$$

where $N$ is the number of sequences in the dataset
$\rightarrow$ Expected number of sequences in the dataset to have a score $\geq x$ $E$-value $\neq P$-value

## Significance of Alignment Scores

$\gg$ How to calculate $K$ and $\lambda$ (in LALIGN and PRSS)

1) The second sequence is shuffiled many times. (simulates random sequences)
2) Smith-Waterman local alignment score is calculated from each alignment: $P\left(S \geq x \mid \mathbf{H}_{0}\right)$
3) The distribution is fitted to an extreme value distribution to obtain estimates of $K$ and $\lambda$
4) P-value is estimated based on the $K$ and $\lambda$, and the original alignment score $x: P(S \geq x) \approx K m n e^{-\lambda x}$ BIOS477/877 L11-13

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## Simulation of Alignment Scores

- RECA ECOLI (P0A7G6; 353 amino acids) - RAD51_YEAST (P25454; 400 amino acids)

Smith-Waterman local alignment score $=293$
(BLOSUM50, gap opening: -10, gap extension: -1 )

| ${ }_{\text {RECA_ECost }}$ |  | 51 |
| :---: | :---: | :---: |
| RR051_yRass |  | 170 |
| Reca_zoorr |  | 94 |
| ${ }_{\text {RaOs5_reass }}$ |  | ${ }^{218}$ |
| Rec__coir |  | ${ }^{135}$ |
| Reast_renss |  | 268 |
| reca__coir |  | 181 |
| R2051_yrass |  | ${ }^{314}$ |
| Reca_zoir |  | ${ }^{228}$ |
| Rno51_reast |  | ${ }_{35}$ |
| R8CA_zolit |  |  |
| Rno51_ zrast |  |  |

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## Significance of Alignment Scores

- Alignment scores cannot be compared directly because they depend on: scoring matrix, gap penalty, algorithms used
- Statistical significance of alignments can be tested
$\rightarrow$ Is the alignment possible just by chance?
$\rightarrow$ If the alignment score is statistically significant (not possible simply by chance), the alignment is meaningful.
$\rightarrow \mathrm{P}$-value or E -value ( $E=N P$ ) can be compared regardless of the scoring systems used for alignments.

NOTE: E-values change depending on the number of data used (if $N$ is small, E -value becomes small)

$$
0<\mathrm{P} \text {-value < } 1 \text { vs. } 0<\mathrm{E} \text {-value < N }
$$

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## Similarity Search

Why do you want to perform similarity search?

- To find related genes in another organisms $\rightarrow$ Homologue candidates
- To identify a possible function of a gene/protein
[From genomic sequence]
- To predict gene structure: against cDNA sequences $\rightarrow$ exon-intron structure
- To predict gene locations

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Heuristic algorithm (FASTA/BLAST)


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FASTA/BLAST Algorithm


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## FASTA/BLAST Algorithm




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FASTA/BLAST Algorithm


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## FASTA Algorithm

1. Find identities using $k$ tuples
( $k$-tuples $=$ words)
2. Join diagonals without gaps
3. Choose top 10 diagonals using a scoring matrix (e.g., BLosum62) init1: the top diagonal score


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## FASTA Algorithm

$>$ Ranking

- Database sequences are ranked based on z-values or OPT scores
$\rightarrow z$-value $=$ the number of standard deviations from the mean (standardized score)
- The high scored sequence pairs are aligned using the full Smith-Waterman dynamic programming algorithm


## $>$ FASTA/SSEARCH website

https://fasta.bioch.virginia.edu/fasta www2/fasta list2.shtmI https://www.ebi.ac.uk/idispatcher/sss/fasta

## [FASTA guide]

https://fasta.bioch.virginia.edu/wro fasta/fasta_quide.pdf.
[William R. Pearson's website]
httts://fasta,bioch.virginia.edu/wroearson/


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## BLAST Algorithm: seeding



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## BLAST Algorithm: seeding

Using words reduce the search space
Neighborhood increases the sensitivity


## BLAST resources

$>$ BLAST

https://blast.ncbi.nlm.nih.gov/Blast.cgi
[Guide to BLAST home and search pages]
ftp://ftp.ncbi.nlm.nih.gov/pub/factsheets/HowTo BLASTGuide.pdf
[BLAST Report Description]
https://ftp.ncbi.nlm.nih.gov/pub/factsheets/HowTo NewBLAST.pdf
[BLAST Statistics]
https://www.ncbi.nlm.nih.gov/BLAST/tutorial/Altschul-1.html
[BLAST Command Line User Manual]
https://www.ncbi.nlm.nih.gov/books/NBK279690/
[BLAST YouTube Tutorials]
(Link is available from NCBI Help page or from Canvas)


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## BLAST Algorithm: seeding




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## BLAST Algorithm: extension



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BLAST Algorithm: extension


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## BLAST Algorithm: Gapped extension

$>$ Gapped extension is triggered after high score ungapped alignments are found


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